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Review

Twenty years of “hot hand” research: Review and critique

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Abstract

Objectives: This article systematically reviews the state of the art of the “hot hand” research in sports. The belief that successive attempts of an individual player are positively related, as well as the behavior influenced by such a belief, will be investigated.

Method: The analysis of experiments, simulations, and archival data from actual sport competitions are structured in a way that evidence for or against the existence of the hot hand is presented. In addition, key issues that have been raised over this debate will be highlighted, including their merits and pitfalls.

Results: The empirical evidence for the existence of the hot hand is considerably limited. Methodological advancements as well as some experimental results indicate a shift in the debate from the adaptiveness of a potentially faulty belief to an adaptive behavior based partly on the hot hand belief.

Conclusions: The potential implications of this review for cognitive theories, empirical studies, and sport practice may provide a significant leverage point for future research and application.

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Keywords: Decision making; Hot hand; Streaks; Review; Sport

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Introduction

In sports a widespread belief exists that success breeds success and failure breeds failure. One major example is the “hot hand” or “streak shooting”—terms that refer to the belief that the performance of a player during a particular period is significantly better than could be expected on the basis of the player’s overall record (Gilovich, Vallone, & Tversky, 1985). In this review we have summarized the literature pertaining to the popular belief in the hot hand phenomenon in sport. We chose to present the more important studies from the last 20 years that have advanced the debate on this issue. The survey is restricted to research related to sport and exercise behavior in its broad sense, rather than general physical activity. Studies done in other academic fields outside the sport domain, such as economics (e.g., Hendricks, Patel, & Zeckhauser, 1993) and cognitive science (e.g., Gilden & Wilson, 1995a), were excluded. Still, it is worth noting that the hot hand debate in sport may well influence other domains and provide boundaries for theories that attempt to explain beliefs and behavior in real environments other than sport.

In the following sections we first present the original report by Gilovich et al. (1985) that stimulated the debate on the hot hand issue, and then review both the supportive and the non-supportive reports that followed it, as summarized in Table 1. Within each category, studies are presented more or less chronologically, so as to follow the development of hot hand research over the years (studies conducted within the same sport field are presented jointly). The origin of the belief in the hot hand is also discussed. We next describe the methodological flaws pointed out mostly by statisticians regarding the efficiency of tests used in those studies (see Table 2). Finally, we demonstrate how the belief in the hot hand affects game strategy and betting in sports. As stated in the literature, there is no one way of writing a review article (see Bem, 1995). However, we believe that organizing the review according to the above categories (i.e., supportive vs. non-supportive studies), as well as demonstrating the methodological and theoretical advantages, may serve as a leverage point for further research.

Our literature review resulted in only two more non-supportive than supportive studies (13 compared to 11, respectively). However, when one closely examines the results, demonstrations of hot hands per se are rare and often weak, due to various reasons: using an unrealistic model and questionable data (Larkey, Smith, & Kadane, 1989), setting questionable definitions for hot and cold players (Forthofer, 1991), relating streakiness to difficulty of task (Gilden & Wilson, 1995b), combining and analyzing data of all players as a group (Stern, 1995), and other constraints related to the kind of sport studied (Frame, Hughson, & Leach, 2003; Klaassen &

Table 1
Summary of the empirical research and real data examination

Study	Sport activity	Database	Results
<i>I.I. Studies that provide evidence against the existence of the hot hand</i> Gilovich et al. (1985)	Basketball	Field goal data for 9 members of the Philadelphia 76ers during the 1980–1981 season. Free-throw data for 9 members of the Boston Celtics during the 1980–1981 and the 1981–1982 seasons. A controlled shooting experiment with 26 members of Cornell's varsity teams.	<ol style="list-style-type: none"> The outcomes of both field goal and free throw attempts were largely independent of the outcome of the previous attempt(s). No significant positive correlation between successive shots was found. The frequency of streaks in players' records did not exceed the frequency expected by a binomial model with a constant hit rate. Players had no more "hot" or "cold" nights (i.e., fluctuations in shooting percentages across games) than would be expected by chance. Players' predictions of their own performance revealed a consistent belief in the hot hand, but the sense of being "hot" did not predict hits or misses.
Siwoff et al. (1988)	Baseball	All baseball games during the 1984, 1985, 1986, and 1987 seasons.	Batting averages were just about as likely to be higher following "cold" streaks as following "hot" streaks (i.e., five games over no more than seven days during which the player batted at least .400 or less than .125, respectively).
Tversky and Gilovich (1989a); See also Gilovich et al. (1985)	Basketball	18 players in 39 NBA games during the 1987–1988 season (only successive shots that were in close temporal proximity).	The results did not support the locality hypothesis (i.e., that the hot hand phenomenon operates only when successive shots are taken within a short time span). The serial correlations were negative for 11 players, positive for 6 players, and the overall mean was $-.02$. None of the correlations were statistically significant.
Tversky and Gilovich (1989b)	Basketball	83 players in 19 NBA games (field goal only).	DiMaggio's sequence of hits is beyond the reasonable expectations of random models. Still, this unique achievement is attributed to DiMaggio's overall high success rate.
Gould (1989)	Baseball	Joe DiMaggio's 56-game hitting streak in 1941.	The hypothesis regarding a time-dependent "hot hand" was rejected: The mean Hit-Hit time interval was larger (though not significantly) compared to a Hit-Miss interval.
Adams (1992)	Basketball	83 players in 19 NBA games (field goal only).	The hypothesis regarding a time-dependent "hot hand" was rejected: The mean Hit-Hit time interval was larger (though not significantly) compared to a Hit-Miss interval.

Table 1 (continued)

Study	Sport activity	Database	Results
Albright (1993a)	Baseball	40 “regular” Major League Baseball players through four seasons, 1987–1990.	<ol style="list-style-type: none"> 1. Some players exhibited significant streakiness during a given season, but this would be expected under a model of randomness. 2. Not a single one of these players exhibited significantly streaky behavior over the entire 4-year period.
Stern and Morris (1993) Comment. See Table 2			
Albright (1993b) Rejoinder. See Table 2			
Frohlich (1994)	Baseball	All American and National Leagues no-hit games occurring between 1900 and 1993.	<ol style="list-style-type: none"> 1. The 202 observed no-hit games since 1900 could be adequately explained if one considers the various factors affecting the distribution of hits/game. 2. The extraordinary high number of no-hitters in the 1990 and 1991 seasons was attributed simply to chance.
Vergin (2000)	Baseball	28 Major League Baseball (MLB) teams over the 1996 season (28 teams \times 162 games = 4536 wins or losses per season).	Wins and losses were shown to be independent of the results of previous games and winning and losing streaks were no longer than would be expected by chance.
Albert and Bennett (2001)	Baseball	29 NBA teams over the 1996–1997 and the 1997–1998 seasons (29 teams \times 82 games = 2378 wins or losses per season).	Zeile exhibited both “hot” and “cold” performances, but the peaks and valleys observed in batting average would be due just to chance.
Clark (2003a)	Golf	The Major League player Todd Zeile’s day-to-day moving average of batting performances over the first half of the 1999 season. 35 professional golfers on the 1997 and 1998 PGA Tour and Senior PGA Tour (18-hole round scores data).	Though a significant trend was found for player’s par or better rounds to occur together and their above par rounds to occur together, the observed streakiness was related to the difficulty of golf courses rather than to any inherent tendency of players to be streaky.
Clark (2003b)	Golf	25 Ladies Professional Golfers’ Association (LPGA) players on the 1997 and 1998 Tours (18-hole round scores data).	The results for the LPGA Tour replicated the findings on the PGA Tour and Senior PGA Tour (Clark, 2003a).

Koehler and Conley (2003)	Basketball	23 shooters in four annual NBA Long Distance Shootout contests, 1994–1997 (a total of 56 sets of 25 shots).	Data gave no evidence for hotness or sequential dependencies.
Gula and Raab (2004) Comment			Koehler and Conley focused only on one of the two plausible interpretations of the hot hand belief. The runs test used in their study is sensitive enough to sequential dependency but less sensitive in detecting non-stationarity.
Clark (2005)	Golf	35 professional golfers on the 1997 PGA Tour. For each player, hole-to-hole scores were analyzed over the entire year and within individual tournaments (a total of 747 tournaments).	<ol style="list-style-type: none"> 1. Significant streakiness over the entire year was found for only three players (one of these players exhibited streakiness in the opposite direction), which is within chance expectations. 2. No player showed a significant tendency for streakiness in individual tournaments.
<i>I.2. Studies that provide support for the existence of the hot hand</i>			
Larkey et al. (1989)	Basketball	18 players in 39 NBA games during the 1987–1988 season (field goal only).	<ol style="list-style-type: none"> 1. The results provided no evidence for the hot hand: Half the players exhibited a positive serial correlation, the other half exhibited a negative serial correlation, and the overall average was essentially zero. 2. Using a contextual approach, it turned out that Vinnie Johnson “the Microwave” was indeed a streak shooter.
Tversky and Gilovich (1989b) Rejoinder	Basketball	Reanalysis of Larkey et al.’s data on 18 NBA players during the 1987–1988 season.	<ol style="list-style-type: none"> 1. The statistical model used in Larkey et al.’s study is unrealistic (since the assumption made about a constant shooting rate is faulty), and thus leading to unjustified conclusions. 2. Vinnie Johnson tended to shoot more after a hit than a miss, but his chances of making a shot were not better following a previous hit. 3. Vinnie’s shooting record was mistakenly coded: his seven-hit streak never happened. When this error is corrected, Vinnie Johnson no longer stands out in the analysis.
Forthofer (1991)	Basketball	Field goal data of 123 NBA players during the 1989–1990 season.	Of the 123 players examined, there were 17 that could be labeled streak shooters (i.e., 5% or more of the total number of games were inconsistent with the player’s season field goal percentage), with an emphasis on three players.

Table 1 (continued)

Study	Sport activity	Database	Results
Gilden and Wilson (1995b)	Golf	Exp. 1: 40 volunteers. Each subject completed one session of 300 putts. Exp. 2: 5 volunteers. Each subject completed three sessions of 300 putts at each of three levels of difficulty (variable putting distance).	Most subjects showed some amount of streakiness (25 of 40 had runs z scores < 0 ; i.e., fewer runs were observed than expected). Streak shooting was observed. However, outcome sequences were streakiest when the difficulty of the task matched to the ability of the performer (i.e., performer's hit rate).
	Golf	Exp. 3: 8 well-practiced and highly trained volunteers. Each subject completed one session of 300 throws at each of three levels of difficulty (variable targets sizes).	1. Dart throwing did not generate solid evidence of streakiness per se. Of the 24 sequences generated, only 1 had a runs z score sufficiently negative, which is within chance expectations. 2. Streaky performance was evident only for intermediate-size targets.
Stern (1995)	Darts	Exp. 4: 4 volunteers. Each subject completed 10 blocks, while a block consisted of 150 trials of each activity.	Only the combined activity (i.e., the mixture of both golf putting and dart throwing data) was moderately streaky.
Adams (1995)	Golf putting and Darts	40 "regular" Major League Baseball (MLB) players through four seasons, 1987–1990. Shot-by-shot scoring for 45 players on the Men's Professional Billiards Association (MPBA) nine-ball tournament. A total of 1464 games were played in 84 matches.	Evidence of streaks was found while players were analyzed as a group rather than individually. 1. The probability of winning a best-of-21 match was significantly greater after having won the first (or first and second) games in the match. 2. The probability of winning a game by running all balls was greater after having won by running all balls in the previous game.
Wardrop (1999)	Pocket billiards	A controlled shooting experiment with a member of the UW-Madison women's varsity team, Katie Voigt (100 shots \times 20 sessions = 2000 attempts).	The results provided statistically significant evidence against the hypothesis of Bernoulli trials with constant (day-to-day) probability of success.
Klaassen and Magnus (2001)	Basketball	Point-to-point data on 4 years of Wimbledon men's and women's singles, 1992–1995, distributed over 481 matches (a total of 86,298 points).	Points were neither independent nor identically distributed (iid): winning the previous point had a positive effect on winning the current point, and at "important" points it was more difficult for the server to win the point than at less important points.
Raab (2002)	Tennis	37,000 rows of sequences of successful spikes and misses for more than 200 players in 226 German first national volleyball league games.	For half of the players a significant autocorrelation between successive shots was found, and was related to high base rates.

Smith (2003)	Horseshoe pitching	64 pitchers (32 men and 32 women) in the 2000 and 2001 World Championships.	Variations in player performances within games and across games were found, which indicated that success probabilities were not completely independent of previous outcomes.
Frame et al. (2003)	Bowling	The Final Round of 1994–1998 PBA tournaments.	The winners of each game won more than 50 percent of their next games, even though they were playing against higher-seeded bowlers.
Dorsey-Palmateer and Smith (2004)	Bowling	43 Professional Bowlers Association (PBA) players on the 2002–2003 season.	Individual success probabilities for many bowlers (i.e., rolling a strike) were neither independent of previous outcomes nor constant across games.
<i>1.3. Inconclusive studies</i>			
Wardrop (1995)	Basketball	Free-throw data for 9 members of the Boston Celtics during the 1980–1981 and the 1981–1982 seasons.	<ol style="list-style-type: none"> 1. Analysis of the collapsed table (as opposite to separate analyses of individual players) gives statistically significant evidence in support of the hot hand phenomenon: a hit was much more likely than a miss to be followed by a hit. 2. The probability of success was not constant: Several Celtics players shot significantly better on their second free throw.

Table 2
Summary of the statistical and methodological observations

Study	Statistical examination and simulated data	Results and conclusions
Kaplan (1990)	<p>The probability that a .300 hitter hits safely in 40 consecutive games is considered, assuming various number of at-bats per game and variability in pitchers' ability.</p>	<p>Using a Bernoulli model to search for hotness in rich contexts as the game of basketball or baseball is an oversimplification that may significantly distort streak probabilities.</p>
Swartz (1990)	<p>$X_1 \sim \text{Bernoulli}(p_1)$, $X_j X_1, \dots, X_{j-1} \sim \text{Bernoulli}(p_j)$, where $p_j = \frac{\sum_{i=1}^{j-1} w_{ji} r_j X_i + p_1 (1 - r_j)}{\sum_{i=1}^{j-1} w_{ji}}$ $w_{ji} > 0$; and $0 \leq r_j \leq 1$.</p>	<p>The chi-square test (used by Tversky and Gilovich 1989a) and the runs test (used also by Gould 1989) are not very powerful in distinguishing small changes from the null hypothesis.</p>
Stern and Morris (1993) Comment	<p>Reanalysis of Albright's data on 40 full-time baseball players available for each of 4 seasons.</p> <p>Simulations (10,000 replications) of player-seasons were conducted, each season consisting of 560 independent batting attempts with probability of success equal to .280. Three alternatives to the Bernoulli model for batters were also considered.</p>	<p>The logistic regression model used in Albright's study has almost no power to detect streak hitting at the individual player level.</p>
Albright (1993b) Rejoinder		<ol style="list-style-type: none"> 1. The negative bias in the logistic regression model, which was found by Stern and Morris, merely indicates that there were slightly more evidence of streakiness than stability across all player-seasons. 2. The logistic regression model should not be able to detect variations, of the kind proposed by Stern and Morris, from the independent Bernoulli model.
Albert (1993)	<p>A Markov switching model using a "moving average" plot is proposed, in which a player switches between two batting averages (a hot or a cold state) from game to game. Within a game, the successive at-bats are independent Bernoulli trials with a fixed success probability. The model was fitted to 50 American League regulars and 50 "random" hitters.</p>	<p>The peaks and valleys observed in the hitting performance of some players would just be due to chance.</p>

- Wardrop (1999)
- The data are 100 Bernoulli trials with probability of success equal to p_B . At some random point, the probability of success increases to p_H , remains at that value for a specified number of trials and then returns to its original value p_B .
- For each of the 38 non-stationarity alternatives discussed, a simulation study with 1000 runs (sequences of 100 trials) was performed.
- The data are 100 dichotomous trials. The first trial is a Bernoulli trial with probability of success p_B . After L or more consecutive successes, the probability of a success is $p_B + \delta$; after L or more consecutive failures, the probability of a success is $p_B - \delta$; otherwise the probability of success is p_B .
- For each of the 36-autocorrelation alternatives discussed, a simulation study with 1000 runs (sequences of 100 trials) was performed.
- Miyoshi (2000)
- Simulated records of shots were created. Each shot was a Bernoulli trial and the probability of successful shots was manipulated to produce sequences of hot-hands shots. One hundred and twenty different scenarios were considered.
- Frame et al. (2003)
- A regime-shifting model in which a basketball player has a fixed probability of switching back and forth between “hot” and “cold” regimes (i.e., success probabilities).
- Dorsey-Palmateer and Smith (2004)
- A simulation model involved a single bowler who had temporary hot and cold spells: During every 7 games there were 10-frame hot and cold periods with respective strike probabilities higher or lower than the bowler’s base rate. The simulated model was replicated 10 million times for each of three different scenarios.
- Burns (2004)
- A program that simulated basketball shooting was designed, based on a Markov modeling. Four parameters were defined: b (bias to give the ball to Player X), h (belief in the hot hand), x (shooting ability for Player X), and y (shooting ability for Player Y). On each trial a player was selected to take the next shot, with a probability of success equal to his shooting
1. None of the seven tests considered in the study (i.e., the runs test, the test of fit, the AC2 test, the AC3 test, and the S_j tests) possesses much power unless the departure from Bernoulli trials is fairly substantial.
 2. In particular, the test of fit is found to be inferior to the other tests at detecting any departure from Bernoulli trials.
 3. While few tests (the runs test, the AC2 test, and the AC3 test) are good at detecting autocorrelation, but poor at detecting non-stationarity—the other tests (the S_j tests) exhibited an opposite trend.
- The runs test and the stationarity test used by Gilovich et al. seem insufficiently sensitive: both tests detected, on average, only 12% of all the hot hands phenomena in the simulated records.
- The runs test has little power to detect non-stationarity of the kind described by the model.
- The three test statistics considered in the study (i.e., the Fisher’s exact test, the number of runs test, and the length of the longest run) are ineffective at detecting non-stationarity.
- Of the 4752 (48 × 99) pairs of simulation runs, only 43 yielded negative advantage scores. Thus, using streaks (i.e., the hot hand belief) as an allocation cue is valid, since this behavior achieves the team goal of scoring more.

Table 2 (continued)

Study	Statistical examination and simulated data	Results and conclusions
Sun (2004)	<p>ability. For each parameter combination, 10 million trials of the hot-hand and of the no-hot-hand simulations were run.</p> <p>A Markov switching model with substantial changes in shooting accuracy (a hot or a cold state) was tested using Gilovich et al.'s field goal data on 16 NBA players. Switching probability was randomly selected from (.95 and .05) with a 50–50 percent chance for every 10 shots.</p> <p>For each player, 10,000 simulations for both the binomial model and the Markov model were performed.</p>	<p>Both the runs test and the MMAC (Max–Min Moving Autocorrelation) statistics indicated that the Markov model was significantly better approximation to the data in comparison to the simple binomial model. Thus, the binomial model is inadequate to serve as a normative model to validate the hot hand.</p>

Magnus, 2001). Whether sequential dependence between events or the non-stationarity argument serve as appropriate descriptions of the hot hand phenomenon depend on the norms applied, as discussed elsewhere (Burns, 2004; Gula & Raab, 2004; Hales, 1999). So far, we think it is safe to say that the scientific support for the hot hand is controversial and fairly limited. Still, the belief is stronger than the reality. As Amos Tversky, who initiated the hot hand research, used to say (cited by Gilovich in an online chat, September, 2002), “I’ve been in a thousand arguments over this topic, won them all, but convinced no one”.

The question whether the hot hand phenomenon does or does not exist remains for the meantime unresolved. From the point of view of the sports scientist there is one important aspect that is worth looking into when judging the relevance of this issue. Saying that there is no hot hand not only contradicts spectators’ and players’ perceptions, but it also goes against a whole body of research (e.g., Bandura, 1997) relating to the role of success and self-efficacy in the enhancement of athletic performance (Bar-Eli & Ritov, 1997; Smith, 2003). Among the diverse sources of efficacy information, enactive mastery experiences (i.e., performance accomplishments) are regarded as the most influential source. According to this theory, a reciprocal relationship between efficacy beliefs and performance outcomes is expected. This idea was used to explain successful streaks within athletic contests, which are usually characterized as shifts in momentum.¹ Moreover, when the same actions (routines) are performed under invariant conditions, adjacent performances are expected to be highly correlated. The fact that Gilovich and his associates (1985) found no evidence for a positive correlation between successive attempts, even under invariant conditions (i.e., free throws in games, or shots taken from fixed positions in training sessions), could be quite problematic for the theory of self-efficacy.

The preliminary hot hand research

The phenomenon of the hot hand is known to everyone who plays or watches the game of basketball. After the player has a run of successful baskets, people tend to believe that he will be more likely to succeed with the next shot as well. This has a plausible causal explanation: When a player feels “hot”, his confidence in his ability increases. He becomes relaxed and focused on performing the shots accurately. So, he “gets in a groove”, such that success in further attempts becomes more likely (Hales, 1999). As Robert Hooke (1989) expressed it so well:

“In almost every competitive activity in which I’ve ever engaged (baseball, basketball, golf, tennis, even duplicate bridge), a little success generates in me a feeling of confidence which, as long as it lasts, makes me do better than usual. Even more obviously, a few failures can destroy this confidence, after which for a while I can’t do anything right” (p. 35).

Such statements assume that athletes’ success probabilities are affected by some kind of physical or psychological state, which, for example in basketball, results in seeing the basket much wider or being “in the zone”. Athletes believe in the hot hand because they have experienced it.

¹Momentum refers to changes in performance based on success or failure in recent events. Terms such as the “hot hand” and “streak shooting” are common examples of perceived momentum. For further discussion of the relationship between psychological momentum and (athletic) performance, see Cornelius, Silva, Conroy, and Petersen (1997), Kerick, Iso-Ahola, and Hatfield (2000), Miller and Weinberg (1991), and Taylor and Demick (1994).

No one doubts that streaks do occur in sports. Obviously, every now and then a professional basketball player may hit a string of nine or ten shots. The key issue in the debate, however, is whether the observed superior (or inferior) performance really deviates from what could occur by chance. Clearly, even random processes such as coin flipping could occasionally result in long streaks of heads or tails. So, an “unusual” performance by an athlete or a team may represent pure statistical probability, or it could be related to a real “streakiness” mood. Supporters of the hot hand strongly believe that even if one accepts the notion that in the world things are often random, there are still some moments in time when athletes act well above or below their norm (i.e., their base rate).

Recently, the norm for deciding whether the hot hand belief is correct or not has been extended beyond comparison to chance. For example, Burns (2001, 2004) argued that the hot hand belief might serve as an adaptive strategy in situations where base rates are unknown or varied, since it leads teammates to allocate the ball to the player with the higher actual shot rate. In line with Burns, Gula and Raab (2004) argued that the hot hand belief is mistakenly judged as being a fallacy due to a scientific norm of randomness, which is less important than the adaptive value of the belief in real decisions. Let us start from the beginning to see how this debate evolved to its current status.

Research on the hot hand started with Gilovich et al. (1985),² a paper originally reported in *Cognitive Psychology* (this research reappeared with slight changes in an article by Tversky & Gilovich in *Chance*, 1989a). Gilovich and his colleagues investigated whether the intuitions of basketball players and fans concerning a hot hand in shooting have any empirical support in actual basketball statistical data. The study begins with a survey that intends to verify exactly what fans believe they are seeing when they say a player has the hot hand. They found that 91% of fans agreed that a player has “a better chance of making a shot after having just *made* his last two or three shots than he does after having just *missed* his last two or three shots”. On average, the differences in hitting probabilities were judged to be nearly 20%; when shooting pairs of free throws, 68% of fans thought that a player has “a better chance of making his second shot after *making* his first shot than after *missing* his first shot”; and 84% of fans believed that “it is important to pass the ball to someone who has just made several (two, three, or four) shots in a row”. Professional basketball players expressed similar beliefs.

In the next stage, Gilovich et al. (1985) translated these common beliefs into a statistical hypothesis that could be tested. They operationally defined “hot hand” using several within-game measures (e.g., analyses of conditional probabilities, run counts, and serial correlations) and one between-game measure (a comparison of the observed and expected variability in shooting percentages across games using the Lexis ratio). This part of the research consisted of three studies in which Gilovich and his colleagues examined the existence of hot hands using three sets of real data: shots from the field of professional basketball players during National Basketball Association (NBA) games; pairs of free throw shots during NBA games; and data from a controlled shooting experiment conducted with men and women varsity basketball players.

Gilovich and his colleagues (1985) found no evidence of the hot hand phenomenon in any of their data sets. Looking at personal shot sequences for nine members of the 1980–1981 Philadelphia 76ers (a total of 3800 shots across 48 home games), it turned out that players’

²A manuscript of this study was already submitted in 1983.

probabilities of making a shot were usually somewhat lower after having made shots than after having missed shots, contrary to the hot hand belief. A comparison of the observed and expected number of runs of hits and misses in the data for each player, across all games and within individual games, also did not support the streak-shooting hypothesis. Moreover, a test of stationarity (i.e., a test which is sensitive to certain fluctuations in hitting probability over time) indicated that there were no more “hot” or “cold” spells in the players’ hit rate than would be expected by chance. A parallel analysis of the field goal records of two other NBA teams, the New Jersey Nets and the New York Knicks, provided evidence consistent with the above findings.

Shots were also independent during free throw shooting of the Boston Celtics and in an experiment with Cornell’s varsity teams.³ In comparison with field goal data, both data sets were considered to be “cleaner”, since they were unaffected by external factors such as players’ shot selection or defensive pressure of the opponents. Still, none of the statistical tests could reliably detect hot hands. Finally, Gilovich et al. (1985) demonstrated that intuition in predicting the outcomes of shots (based on patterns of successes) was faulty, as the outcomes of previous shots influenced Cornell players’ predictions (expressed in the form of a betting game), but not their performance.

Obviously, Gilovich et al. (1985) did not wish to claim that basketball shooting is a purely chance process, like coin tossing. There is very little about basketball performance, of course, that is random. The data merely indicate that the chances of hitting a given shot (i.e., a player’s hit rate) are largely independent of the player’s prior performance. Yet the outcomes of previous shots may well have an effect on a player’s willingness to take the next shot. As a result, a player may score more points in one period than in another, not because of real changes in his performance level (i.e., shooting accuracy), but simply because he shoots more often (Tversky & Gilovich, 1989a).

In another study, Tversky and Gilovich (1989b) reported on an additional analysis in a new data set (which was collected originally by Larkey et al., 1989). They computed for each player the serial correlation for all pairs of successive shots separated at most by one shot of another player on the same team. The time span between shots is generally less than a minute and a half. Still, the results did not support the locality hypothesis: Correlations’ overall mean was .02, and none of the values was statistically significant.

Gilovich et al.’s (1985) basketball shooting research has generated a sizable number of follow-up studies and further analyses and critiques. Research on the hot hand has been extended beyond the original sport studied, basketball, to other sports, including baseball (Albert & Bennett, 2001; Albright, 1993a; Frohlich, 1994; Gould, 1989; Siwoff, Hirdt, & Hirdt, 1988; Stern, 1995; Vergin, 2000), volleyball (Raab, 2002; Raab, Gula, & Gigerenzer, submitted), golf (Clark, 2003a, b; Clark, 2005; Gilden & Wilson, 1995b), tennis (Klaassen & Magnus, 2001), bowling (Dorsey-Palmateer & Smith, 2004; Frame et al., 2003), darts (Gilden & Wilson, 1995b), pocket billiards (Adams, 1995), and horseshoe pitching (Smith, 2003). It has also generated a great deal of interest among researchers in other academic fields (such as economics, cognitive science, law, and even religion).

³Gilovich et al. (1985) reported that only one player out of 26 exhibited a significant positive correlation, which we might expect just by chance. For a different interpretation of the results obtained in this experiment, see Wardrop (1998).

Evidently, the intuition that Gilovich et al. have challenged is strong enough to keep the research on the topic in motion.

The origin of the hot hand belief

Gilovich et al. (1985) suggested that the consistent belief in the hot hand could be due to a memory bias. If streaks are more memorable than alternations, the observer is likely to overestimate the correlation between successive shots. However, they favored another possible explanation. They attributed the discrepancy between the observed basketball statistics and the intuition of knowledgeable observers to a general misconception of the laws of chance, whereby even short random sequences are expected to be representative of the process that generates them. In other words, people often disregard sample size when making judgments and predictions. This cognitive bias has been described previously by Tversky and Kahneman (1971, 1974), and is known as “the belief in the law of small numbers”. While watching a random process, people usually expect more alternations and fewer long streaks than actually occur, and thus tend to “detect” patterns (i.e., streaks) even where none exist (Tversky & Gilovich, 1989a).⁴ A similar interpretation relating to people’s inability to perceive randomness was also offered by Falk and Konold (1997). So, in the game of basketball the hot hand fallacy appears to be a purely mistaken notion about the distribution of hits and misses (Gilovich, 2002).

Few researchers have questioned Gilovich et al.’s (1985) deductions. Gigerenzer (2000) pointed out that explaining the gambler’s fallacy (i.e., a streak of events is likely to end; this phenomenon was first described by Laplace, 1814/1951) and the hot hand fallacy (i.e., a streak should continue) with the same principle raises problems. Yet, both of these opposing phenomena have been attributed to the “*representativeness*” heuristic. Amazingly, this one-word explanation accounts for both A and non-A. Ayton and Fischer (2004) expressed similar observations and proposed alternative accounts for these two opposing expectations. They empirically demonstrated that sequence recency (i.e., binary sequences with different alternation rates; positive vs. negative recency) influences subjects’ attributions that human performance or chance generated the sequence. Burns and Corpus (2004) argued that critical to how streaks are interpreted are people’s judgments about the underlying process generating the events. A manipulation check confirmed Burns and Corpus’s predictions that people are more likely to follow streaks when the mechanism generating events is judged to be non-random than when the generating mechanism is judged to be random.

In line with the above arguments, Caruso and Epley (2004) claimed that predictions about the continuation of a streak depend on perceptions of the agent’s intentions. Thus, the hot hand should emerge in contexts involving intentional agents (i.e., humans) where events are perceived to be dependent on one another; streaks indicate intentional actions that should continue. In other contexts involving unintentional agents (i.e., machines), such as the gambler’s fallacy, streaks represent random accidents that are unlikely to continue.

⁴Recently, a brain study by Huettel, Mack, and McCarthy (2002) demonstrated that specific areas of the brain are activated by streaks, and that the strength of the signal is related to the length of the streak.

The validity of the hot hand belief

Studies that provide evidence against the existence of the hot hand

Since Gilovich et al.'s original report was published in 1985, most of the subsequent research has continued to consist of statistical tests of actual sports data in an effort to determine if there are sports where a hot hand can be detected. While most of the research has concentrated on either finding support or rejecting the existence of the hot hand using archival and simulated data sets (so as to improve methodological concerns), theoretical improvements have been almost neglected, and have not been systematically and experimentally examined (see Burns, 2004 for an exception). Meanwhile, both common interpretations of the hot hand belief, either sequential dependence between successive attempts or the non-stationarity claim, have been extensively examined, particularly in basketball and baseball.

Siwoff et al. (1988) reported their own study of streakiness in the game of baseball for the 1984–1987 seasons. They calculated the batting averages of players in games right after a “hot” or a “cold” streak (defined as a sequence of five games over no more than 7 days during which the player batted at least .400 or less than .125, respectively), and compared these batting averages to the players' overall record. They found that batting averages were just about as likely to be higher following cold streaks as following hot streaks.

Albright (1993a) analyzed streakiness in batting by examining 501 season records of professional baseball players through four seasons (1987–1990). His analysis used logistic regression to incorporate situational effects on hitting into his model (e.g., pitcher's Earned Run Average, pitcher's handedness, home/away status of the game, and night/day status). Statistical association between outcomes of successive at-bats was tested, while the other extraneous factors were held constant. Using several years of data, it was also possible to test whether certain players were particularly streaky, or if perhaps streakiness tends to be a one-season phenomenon. Albright found that while some batters exhibited streakiness in some seasons (e.g., Dwight Evans in the 1988 season), they did not do so consistently, and the number of runs in the data (sequences of successful at-bats or unsuccessful at-bats) did not significantly deviate from randomness. Frohlich (1994) reported on similar results for strings of consecutive hits (actually, the incidence of no-hit games was of interest in this study) in baseball, at the team level.

Commenting on Albright's article (1993a), Stern and Morris (1993) argued that no convincing evidence of streaks was found in the data, due to the small effect sizes and a bias in logistic regression that offset the small effect. Albert (1993) proposed a Markov switching model, in which a player switches between two batting averages from game to game. However, such a model did not lead to the conclusion that streakiness does in fact exist in batting (interested readers should refer to Albright's (1993b) rejoinder).⁵ Stern (1995) suggested that evidence of streaks exists in Albright's data, if players are analyzed as a group rather than individually.

Gould (1989) stated that hitting streaks in baseball do not exist, with a single exception—Joe DiMaggio's 56-game hitting streak during the 1941 season. This remarkable record has never

⁵Elsewhere, Albert and Williamson (2001) analyzed Javy Lopez's pattern of hitting across games for the 1998 major league baseball season, using the Markov switching model. Contrary to the belief that Lopez was streaky during this season, the model was unable to pick up any significant streakiness.

been challenged (Wee Willie Keeler's record in 1897 and Pete Rose's record in 1978, both with 44, come in second). Gould attributed the faulty belief in the hot hand to an inherent disability in human beings, saying, "our minds are not built (for whatever reason) to work by the rules of probability, though these rules clearly govern our universe" (p. 15).

Albert and Bennett (2001) used a computer simulation to replicate the famous streaky hitter Todd Zeile's game performances over the first half of the 1999 season. The results of this simulation showed that the peaks and valleys in Zeile's batting average could simply occur due to chance. Albert and Bennett suggested that one should be careful about labeling someone a streaky hitter, since chance is a very powerful force in creating streaks.

Back to basketball, Adams (1992) argued that looking only at the sequences of shots without looking at how far apart in time the shots occurred could possibly lead to missing the hot hand. Yet, he found that the mean interval between two consecutive successful shots made ($t_1 = 17.04$ s) during 19 NBA games was slightly longer than the mean interval between a shot made and a shot missed ($t_2 = 16.39$ s). A difference that is opposite, though not significantly, one expected by a time-dependent hot hand hypothesis. (Note that elsewhere, Adams (1995) found some evidence of hotness in the play of professional tournament pool players. Still, he considered the hot hand/streaks issue to be far from resolved.)

Vergin (2000) extended the exploration of the hot hand by looking for momentum over the length of a season. Actual winning and losing streaks for 28 major league baseball teams and 29 NBA teams were compared to streaks that would have occurred under the assumption that game outcome is independent of the results of previous games. In fact, both the chi-square goodness-of-fit test and the Wald-Wolfowitz runs test for randomness showed a very close fit of observed streaks to expected streaks under the independence assumption. It seems that contrary to the prevalent belief in momentum and streaks, the probability of a win or loss was simply unrelated to the team's performance in its recent games. Despite the results of this research, Vergin (2000) emphasized the fact that "winning in baseball, basketball and other sports is not simply a random event. They are games of skill and the better teams win more often than the inferior teams" (p. 195). He acknowledged that although every now and then winning and losing streaks are observed, "the data demonstrate that such streaks are no more frequent or persistent than would occur by chance, given teams' overall strengths" (p. 195).

For hotness studies, Koehler and Conley (2003) suggested that the NBA Long Distance Shootout contest is a superior context in comparison to free throws. They claimed that the former is a more appropriate setting for perceived hotness (i.e., difficult shots, short time span, three-shot run), while it closely reflects various NBA game conditions (e.g., professional players, competition, professional court, large crowd). The Long Distance Shootout is an annual contest that pits eight of the best 3-point shooters in professional basketball against one another. By comparing expected and actual runs, Koehler and Conley detected no unusual streaks of success and no sequential dependency in the performance of 23 participants in four annual contests (1994–1997), except for two players, Nick Anderson and Dennis Scott. A review of spontaneous outbursts by the contest announcers about players who are "on fire" also failed to reveal evidence of hot hands.

In their comment on Koehler and Conley's (2003) study, Gula and Raab (2004) agreed with the results but presented an alternative interpretation that evaluates the rationality of beliefs and its adaptiveness in behavior. The link between belief and behavior may arise in situations where a

faulty belief in the hot hand results in an adaptive behavior. For instance, if base rates are unknown or of a high variability, the perceived hotness of a player may assist other players in the game in detecting the best shooter. Accordingly, if the value of the belief in the hot hand is being judged, then one should distinguish between the cognitive level of the phenomenon (the hot hand belief) and the behavioral level (favoring the hot player). Since Koehler and Conley focused on only one of the two cognitive level criteria, i.e., the dependency of hits but not on non-stationarity, their results may have quite limited value if practical conclusions regarding behavior are to be drawn.

Studies that provide evidence in favor of the hot hand

Larkey et al. (1989) challenged Gilovich et al.'s (1985) conclusions and continued to search for the hot hand. In a new data set they collected, Larkey and his colleagues analyzed the records of 18 outstanding players across the 1987–1988 NBA season. The results actually replicated Gilovich et al.'s findings: Half the players exhibited a positive serial correlation between successive shots, while the other half exhibited a negative serial correlation, thus providing no evidence for the hot hand.

Larkey et al. (1989) dismissed these results on the grounds of both statistical and conceptual (or contextual) arguments. They pointed out that extracting individual player sequences of hits and misses from an actual game is too complicated a task, and that analysis should be restricted to “cognitively manageable chunks of shooting opportunities” (p. 24). Therefore, they limited consideration to streaks that occurred during a short period within a game (i.e., sequences of 20 baskets). Using a descriptive analysis method, it turned out that Detroit's Vinnie Johnson, “the Microwave”, was indeed a streaky shooter, and hence the hot hand does exist. In their concluding remarks, Larkey and his colleagues rehabilitated the faith in our ability to make proper reasoning and stated that it is OK to believe in the hot hand.

Since Larkey et al.'s (1989) argument in favor of the hot hand was based on the performance of a single player in a single observation (i.e., a run of seven consecutive hits within a 20-shot sequence during the fifth Piston–Laker playoff game), Tversky and Gilovich (1989b) considered this conclusion to be hardly convincing. Most importantly, they revealed an error in Vinnie Johnson's shooting record coded by Larkey and his associates (the 7 out of 7 sequence by Johnson turned out not to have happened!), which caused the whole case for the Microwave to “go up in smoke”.

Forthofer (1991) used newspaper box scores (i.e., the game summary of shots taken and made by each player) to examine all NBA players in all games during the 1989–1990 season. This database documented the record of 123 men who played in 50 or more games and averaged more than nine shots per game. Forthofer's main idea was to identify the most extreme players, and therefore he classified streak shooters into one of three categories: those with “hot and cold streaks”, those with “hot hands”, and those with “cold hands”. For a player to be classified as a streak shooter, his record in 5% or more of the total number of games played had to be inconsistent with his season field goal percentage. Eventually, of the 123 players examined, 17 players exhibited some form of streakiness, with an emphasis on three players.

Wardrop (1998) highly praised Forthofer's idea, but at the same time criticized his criterion for labelling the streakiest shooters. Wardrop pointed out that if we eliminate the “shaky” cases in

Forthofer's results, we are left with only 10 players, not 17 who exhibited some form of streakiness. He also suggested that the same analysis should be repeated over several years to see whether the set of players exhibiting streakiness will be fairly constant.

In an earlier study, Wardrop (1995) reexamined the free throw data presented by Gilovich et al. (1985) (i.e., free throw data for nine members of the 1980–1981 and 1981–1982 Boston Celtics teams) and suggested a different interpretation of the data. He showed that if the data are aggregated over players, then fans' perceptions of hot hand in free throw shooting are correct: Players made a basket 79% of the time after a hit compared to 74% of the time after a miss. He also showed that the Celtics players, as a group, were better free throw shooters on their second attempt than on their first attempt. Wardrop considered it difficult to assume that any basketball fan has a separate 2×2 contingency table for each of the hundreds, if not thousands, of players he or she has seen play. It seems much more reasonable to assume that a fan has a single 2×2 table in mind only for the aggregated data. This mental equivalent of Simpson's paradox (Simpson, 1951) could lead to a cognitive statistical illusion that results in "detecting patterns even where none exist". In other words, aggregation does not provide any evidence for the existence of the hot hand, but merely helps us to understand why the fans believe what they do.

Gilden and Wilson (1995b) presented some experimental evidence of streakiness in golf putting and darts, and showed that streak magnitude is closely associated with task difficulty, i.e., performer's hit rate. They also suggested that the time delay between trials could somehow explain the negative results reported by Gilovich et al. (1985) in the context of free throw shooting. Smith (2003) criticized Gilden and Wilson's results for their artificiality, explaining that their experiments involved volunteers performing 300 repetitions and being paid \$5 plus 5 cents per hit. Smith argued that with so many trials and such small payment, no wonder that there were substantial fluctuations in the attentiveness of the poorly motivated volunteers.

Clark (2003a) investigated the occurrence of streakiness among professional golfers on the PGA Tour and Senior PGA Tour over a 2-year period. Whether players were examined individually or as a group, there was a significant tendency for players' par or better rounds (i.e., good performance) to cluster together and also for players' above par rounds (i.e., poorer performance) to cluster together. However, an additional analysis showed that the observed streaks were related to the difficulty of the golf courses rather than to any inherent tendency of players to be streaky. The results for the PGA Tour and Senior PGA Tour were extended later to the Ladies Professional Golfers' Association (LPGA) Tour as well (Clark, 2003b). In another study, Clark (2005) reported on the results of a hole-to-hole scores analysis for the same 35 players on the 1997 PGA Tour. For each player, raw scores were converted to par or better and above par, and were arranged in a 2×2 contingency table. Whether one is interested in streakiness in individual tournaments or over the entire year, no evidence for a hot hand was found. The data on hole-to-hole scores strongly suggested that past performance is not a good predictor for future behavior.

Klaassen and Magnus (2001) used almost 90,000 points (481 matches) at Wimbledon from 1992 to 1995 to investigate whether points in professional tennis were independent and identically distributed (iid). They found that unlike basketball, winning the previous point in tennis had a positive effect on winning the current point, and at "important" points it was more difficult for the server to win the point than at less important points. Moreover, the stronger the player the weaker were these effects, for both men and women. For example, average players in the men's

singles were expected to win approximately 65% of their service points. If the previous point was won (and if the current point was not the first point in the game), then the probability of winning a point increased by .3%, reflecting a “winning mood”. However, if the previous point was lost, the probability of winning a point decreased by .5%. At a point of zero importance, the probability of winning a point on service increased by .4% compared to a point of average importance. Klaassen and Magnus showed that the divergence from the iid model was so small, it could still provide a good approximation in many practical applications concerning tennis.

Then again, the possibility can be raised that in games such as tennis, one cannot determine whether an unusual performance is due to one player playing exceptionally well or the other playing badly, or the combination of the two (Adams, 1995). It is also worth noting that earlier studies of tennis reported by Richardson, Adler, and Hankes (1988) and Silva, Hardy, and Crace (1988) found only limited support for a momentum effect. For other related aspects of independence and identical distribution of points in tennis, see Croucher (1981), Jackson and Mosurski (1997), and Magnus and Klaassen (1999a, b, c).

Smith (2003) argued that Gilovich et al.’s (1985) basketball data do not control for several confounding factors (e.g., shot selection, lengthy spells between shots, and strategic adjustments). He found horseshoe pitching data to be much cleaner, since every pitch is made from the same distance at regular intervals, with intense concentration and no strategy. An analysis of horseshoe pitching data from the 2000 and 2001 World Championships indicated that world-class pitchers do have modest hot and cold spells. Men and women were both somewhat more likely to throw a double after a double than after a non-double and were also more likely to throw a double after two doubles in the preceding two innings than after two non-doubles. Such variations in players’ performances within games and across games provide evidence that success probabilities are somewhat affected by previous outcomes.

Frame et al. (2003) found evidence of hot hands in bowling using data from the Final Round of 1994–1998 Professional Bowlers Association (PBA) tournaments. During these years, the Final Round involved step-ladder matches in which winners of each game moved on to play against higher seeded bowlers in their next games. The results indicated that the winners of each game won more than 50% of their subsequent games, even though they were competing against higher seeds. However, these results could be partly attributed to the effort exerted by the lower seeds who had to bowl continuously while the higher seeds were waiting for their turn to play.

Dorsey-Palmateer and Smith (2004) examined professional bowling data from the 2002–2003 season, searching for streakiness in performance. Unlike Gilovich et al. (1985), they found that for many bowlers, the probability of rolling a strike (i.e., all 10 pins are knocked down on the bowler’s first throw) was not independent of previous outcomes and the number of strikes rolled varied more across games than could be expected by chance. For example, most bowlers had a higher strike proportion after rolling one-to-four consecutive strikes than after rolling one-to-four consecutive non-strikes, and this difference became more significant as the number of trials increased from one to four.

Hales (1999) offered an epistemological observation to the hot hand in sports. In his paper, he defended the view that hot hands do exist, and that players and spectators are often correct in identifying them. Hales suggested that any streak or run of success should be considered as a hot hand, with no arbitrary restrictions on how rare or improbable it must be. Thus, if Michael Jordan hits 10 free throws in a row, he *does* have a hot hand, even if statistically this is a

conceivable occurrence given his skill as a player and his experience in free throw shooting. Having the hot hands simply represents above-average success runs: people are “shooting above their norm, serving better than average, punting deeper than usual, deviating above the mean” (p. 84).

The hot hand test statistics

Gilovich et al. (1985) stated that in statistical terms, fans’ perceptions of the hot hand exhibited non-stationarity and serial dependence. They used four different types of statistics to analyze each player’s sequence of hits and misses: the proportion of successful shots, conditioned by the success or failure of the previous shot(s); the first-order correlation coefficient; the number of runs in the data using the Wald–Wolfowitz runs test; and the number of successful, moderately successful, and less successful series of consecutive shots, in blocks of four. To check stationarity, a chi-square test was performed on successive blocks of four shots.

An important question to be asked is whether Gilovich et al.’s (1985) research provides enough evidence to reject the existence of the hot hand phenomenon in basketball. Is it possible that their findings are valid but hot hands still exist? Few researchers decisively argue that the statistical power of Gilovich et al.’s analyses may have been insufficient. Kaplan (1990) argued that Tversky and his associates mistakenly based their conclusions on a Bernoulli model independent, identical trials. Using such a model to search for hotness in rich contexts such as the games of basketball and baseball is an oversimplification that may significantly distort streak probabilities. Swartz (1990) illustrated that the statistics used by Gilovich et al. (in particular, the chi-square test) were not very powerful in distinguishing the null hypothesis (i.e., the non-existence of the hot hand) from some other alternatives.

The binomial model (usually referred to as the *coin-tossing model*) assumes that for each player, shooting trials are independent, and that the probability of success is constant over trials. Gilovich et al. (1985) focused on independence as the leading argument in opposition to the hot hand belief in sports. Since the publication of their results, the claim of sequential dependence has been extensively studied; it seems that researchers do share the notion that consecutive successful shots are often not positively associated. However, another possible interpretation of this belief suggests that players’ performance fluctuates over time and that hit rates are not constant (i.e., the non-stationarity claim; see Gula & Raab, 2004; Hales, 1999; Raab, 2002). For instance, a basketball player’s success probability might be 0.5 for 15 trials, then suddenly change to 0.6 for 8 trials, and then return to 0.5 for the next 15 trials. In such cases, the simple binomial model may not be a proper normative model for evaluating the validity of the hot hand belief.

Few researchers strongly believe that streaks do occur, however, both the magnitude of the phenomenon and statistical tests in use are often so weak that streaks can hardly be detected. Studies by Dorsey-Palmateer and Smith (2004), Miyoshi (2000), and Wardrop (1999), and a working paper by Frame et al. (2003), all demonstrate that standard hot hand tests are unable to detect non-stationarity and changes in the success probability.

Wardrop (1999) addressed the question of whether Bernoulli trials are a suitable model for the outcomes of successive shots in basketball. He reported on a large simulation study using a specific model of non-stationarity: The data consisted of a sequence of 100 Bernoulli trials with

probability of success equal to p_B (for example $p_B = 0.5$). At some random point, the athlete gets hot and the probability of success increases to a value $p_H > p_B$ for a specified number of trials (for example, $p_H = 0.7$ for the duration of 10 trials). Afterwards, the probability of success returns to its original value p_B for the remainder of the sequence. Wardrop found that both the runs test and the test of fit used by Gilovich et al. (1985) had little power to detect departures from Bernoulli trials (i.e., non-stationarity) unless p_H was much larger than p_B . In fact, he concluded that the test of fit was worthless and hence it should not be used.

Frame et al. (2003) presented a model in which a player has a fixed probability of switching back and forth between “hot” and “cold” regimes.⁶ They demonstrated that the runs test has little power to detect non-stationarity in such a regime-shifting model. Dorsey-Palmateer and Smith (2004) examined the power of several tests (specifically, the Fisher’s exact test, the number of runs test, and the length of the longest run) by using a model in which bowlers had temporary hot and cold spells. They emphasized that test statistics with relatively few observations are often largely ineffective unless extreme violations of the binomial model’s assumptions are present.

Miyoshi (2000) used simulations to suggest that the sensitivity of tests used by Gilovich et al. (1985) depends on four variables: the frequency of hot hand periods in a season, the total number of hot hand shots in the season, the number of shots in each hot hand period, and the size of the increase in the probability of success in hot hand periods. He demonstrated that when the values of these variables were set realistically, Gilovich et al.’s tests (i.e., the runs test and the test of fit) could detect, on average, only 12% of all the hot hands phenomena in the simulated records. Therefore, Miyoshi urged us not to reject the existence of the hot hand in basketball merely on the basis of Gilovich et al.’s findings.

Hooke (1989) emphasized the inherent difficulty of using statistical methods to study complicated situations, such as the game of basketball or baseball. According to his own intuition “the alternative hypothesis is not that there is a ‘hot hand’ effect that is the same for everyone, but that the real situation is much more complex”. Consequently, “a measure that is appropriate in detecting the effect for one of these types [of hot- hands] may not be very powerful for another” (p. 36). It appears that the issue is much more complicated than Gilovich et al. made it out to be.

Implications of the hot hand belief

One relevant demonstration for the hot hand belief effect is related to betting in sports. Camerer (1989) examined whether perceived hotness affected the point spreads in the sports betting market. He found that bets placed on teams with winning streaks were more likely to be *losers* rather than winners (while losing-streak teams performed better than expected), and thus he concluded that the basketball market believes in the hot hand even though it does not exist. The biases were minor, however, and of marginal statistical significance. In a comment, Brown and Sauer (1993) suggested that the changes be documented in both point spreads and team

⁶Hot and cold regimes differ from one another in success probability. For example, an athlete might always have a 0.25 probability of switching between a “hot” regime with a 0.6 success probability and a “cold” regime with 0.3 success probability.

performance stemming from streaks. Still, their results were inconclusive about whether the hot hand is a myth or a firm reality.

Another demonstration for the hot hand effect is related to game strategy. Gilovich (1984) described several general biases and showed how they lead to faulty conclusions in the world of sports. Some of these biases produce misconceptions, such as the belief in the *Sports Illustrated* jinx,⁷ and have no harmful consequences. Other misconceptions may lead to unfortunate decisions, as in the case of the sophomore slump⁸ (Taylor & Cuave, 1994) and the belief in the hot hand. Acting on the basis of the hot hand belief has several possible implications for how coaches use their players, how teammates pass the ball during the game, and how willing the players are to take the next shot. Tversky and Gilovich (1989a) pointed out the direct consequences that such a fallacy may have on basketball game strategy: “Passing the ball to the hot player, who is guarded closely by the opposing team, may be a non-optimal strategy if other players who do not appear hot have a better chance of scoring” (p. 21). Thus, like other cognitive illusions, “the belief in the hot hand could be costly” (p. 21). Elsewhere, Gilovich (2002) emphasized that teams win games by having their shots taken by their best players from the best positions on the floor, while preventing the opponents from doing the same. He doubted whether the erroneous belief that hits tend to be followed by hits and misses by misses could serve such an effort.

Burns (2004) presented evidence that under specific circumstances, base rates may well be inferred from the runs of hits in a player’s performance. In an earlier article, Burns (2001) pointed out that the irrational belief in the hot hand might be an effective, fast, and frugal heuristic for deciding how to allocate the ball between members of a team (even if shots really are independent events). Since the number and length of streaks of successive hits is greater for those players with a higher shooting percentage, it may well serve as a valid cue for detecting the best shooters. Moreover, when the hot hand belief is used for allocation decisions, Burns (2004) calculated an advantage of about one extra basket per seven or eight games, which may result in winning or losing a game. However, such an adaptive approach assumes that teammates cannot find the best players without this cue of “hotness”. Obviously, better cues do exist, especially when one is speaking about professional NBA players.

Gula and Raab (2004) discussed the relationship between base rates and streaks of hits perceived as unusual. In light of the above arguments, they recommended that coaches and players incorporate both the hot hand information and other available indications (e.g., base rates, strength and weakness of opponent’s defense, trained tactics), so as to increase a team’s probability of winning. However, whether the hot hand information or the base rate is to be used depends on the environmental structure. For instance, it is likely that base rates and the hot hand are positively correlated. In addition, it seems plausible that the base rate is a good predictor for success in a game. Given that these two pieces of information are ordered by their validity, using the highest valid information (cue) could be quite successful. Whether only one piece of information or several cues are needed depends on the cue–cue correlation as well as on the

⁷A superstitious belief about athletes or teams having bad luck after their picture appears on the cover of *Sports Illustrated* magazine. Such a belief is associated with the failure to recognize regression effects in athletes’ performances.

⁸The term refers to an athlete’s atypically good performance in his rookie year, which is followed by a deterioration in performance during the subsequent year. Despite the fact that this phenomenon is generally the result of statistical regression, people tend to believe that factors such as a sophomore jinx or a player being overconfident are responsible for the poor performance.

cue–criteria correlation, as pointed out elsewhere (see Gigerenzer, Todd, & The ABC Research Group, 1999, for an overview).

Discussion

Task segregation

Basketball and baseball studies dominate the hot hand literature. In comparison with basketball and baseball, other sports are considered to have more valuable properties for detecting streakiness in performance. For the present study, the main parameter to distinguish between the different sports is related to the individual-player envelope conditions when performing the counted task. In basketball, players make their shots from different distances and angles under different defense conditions, and in baseball, batters play against pitchers of different abilities. In golf, darts, or bowling, some confounding factors related to team play, shot selection, defensive pressure, or other strategic considerations are expected to have almost no influence. It is therefore important to examine whether support for the hot hand was mostly found in the latter kinds of sports, and how significant was the effect.

Evidently, grouping and analyzing the studies in Table 1 according to such a criterion (see the “sport activity” column) could hardly lead to a firm conclusion regarding the relationship between the hot hand and the type of sport studied. In some studies, hot hands could not be detected, even in sports or tasks that *are* performed in relatively “pure” settings, such as golf (Clark, 2003a, b; Clark, 2005), three point basketball shooting (Koehler & Conley, 2003), free throw shooting (either in games, or shots taken from fixed positions in a controlled experiment, as reported by Gilovich et al., 1985), and darts (Gilden & Wilson, 1995b). However, it is worth noting that the strongest support for the hot hand was found in the more “individually” performed sports (as opposed to team-sports), namely horseshoe pitching (Smith, 2003), bowling (Dorsey-Palmateer & Smith, 2004), and to a certain extent tennis (Klaassen & Magnus, 2001). Moreover, even if the failure to find hot hands in basketball shooting is attributed to the nature of the task being performed (i.e., a closed skill, fine motor task that requires a narrow focus of attention), such an argument still has no power to explain why evidence for the hot hand from a number of studies in baseball (Albert & Bennett, 2001; Albright, 1993a; Frohlich, 1994; Siwoff et al., 1988; Vergin, 2000) was also elusive.

While reviewing the hot hand literature, we evaluated the quality of the results obtained from real data and various empirical studies. Several parameters were considered, such as the sample size (number of participants), the control level of relevant confounding variables, the volume of data collected, the power of the statistical methods employed, and most important, the significance of the results obtained. High-quality data are no doubt needed, and evidently are seldom found. Among the more well-designed studies we found the non-supportive hot hand prominent studies of Gilovich et al. (1985) and Tversky and Gilovich (1989b) in basketball; Albright (1993a), Vergin (2000), and Albert and Bennett (2001) in baseball; and Clark (2003a, b) and Clark (2005) with men and women golfers. On the supportive side, studies by Smith (2003) and Dorsey-Palmateer and Smith (2004) in horseshoe pitching and bowling, respectively, provided strong support for the hot hand, along with the Klaassen and Magnus (2001) study in

tennis. It should be pointed out, however, that in the above-mentioned studies all participants were professional athletes.

This review follows the hot hand debate over the years. The gap between belief and reality is what makes this issue so exciting. People are convinced that the effect exists because they strongly feel it, although the majority of well-designed studies could not provide evidence even for a small significant effect. The extreme discrepancy between intuition (or expectations) and statistical results from a variety of sports is indeed astonishing. In any case, the hot hand effect size must be much smaller than athletes and fans believe. Yet, it is possible that hotness does exist, but specific variables related to the person performing the task (e.g., level of expertise, level of arousal), the nature of task being performed (e.g., type of sport, level of accuracy needed), or the environment in which the task is being performed (e.g., competitive atmosphere) interact so as to influence its detection. The combination of variables essential for the hot hand to emerge perfectly is still to be explored, and hence, any progress toward this challenge might be of a great value.

Hot hand definitions

The hot hand body of research has certainly evolved in the last 20 years. Still, the main interest has been focused on the question of whether hot hands exist or not, based on the same operational definitions of hotness (and measures) proposed in the original study by Gilovich and his colleagues. Ninety-one out of 100 basketball fans expressed a belief that a player's future success depends on the results of his prior attempts. A statistical description of the hot hand phenomenon using the term $p(\text{hit}/\text{hit}) > p(\text{hit}/\text{miss})$, usually combined with the runs count test, has become the standard in hot hand research. The issue has rarely been addressed in a different manner so as to advance the debate, with Hales's perspective being an exception.

Hales (1999) suggested that the common necessary conditions of having hot hands be rejected, namely: (a) that a player should perform in a way that "success breeds success"; (b) a streak of success should statistically be unlikely (e.g., Joe DiMaggio's 56-game hitting streak in 1941); and (c) the number of successes in a row must exceed that predicted by chance. Once no such properties were found in real sports' data, researchers (erroneously) concluded that there are no hot hands and that everyone is wrong in thinking otherwise. Instead, Hales argued that "being hot does not have to do with the fecundity, duration, or even frequency of streaks. It has to do with *their existence*" (p. 86). When one believes he has a hot hand, he may well be usually right.

Such an epistemological point of view is surely unique and refreshing, though we suspect that most researchers would not agree with it. However, if one considers the hot hand as not being a serial dependence between trials, an extreme statistical unlikeliness of streaks, or an occurrence which is beyond the laws of chance—then how else should it be described and measured? Hales (1999) and other researchers (Gula & Raab, 2004; Raab, 2002) put it simply, saying that a player has a hot hand when he is playing better than average. Well, if a streak could end at any time, the non-stationarity claim, i.e., occasional fluctuations in a player's hit rate, seems to serve as an adequate description of hotness; however, valid solutions (other than the simple model of Bernoulli trials, as suggested by Sun, 2004) are needed to model it. Moreover, we believe that focusing only on the sequential dependence criterion ("*an omnipresent effect*", see Wardrop, 1998) and ignoring the non-stationarity argument ("*an occasional effect*") would result in a non-sufficient definition of hotness, which might distort the nature of the phenomenon.

Practically, which of the two criteria used depends on the norms applied. From a behavioral point of view, the adaptive value of the belief in real decisions is more important than the normative validity of the belief. Burns (2004) demonstrated that a team's chances of winning a game were higher if the ball was passed to the "hot" player more often than according to players' base rates, even if such a strategy is based on a faulty belief. Therefore, we suggest that the hot hand should be judged neither as being a fallacy nor as an adaptation, but as information to be used together with other cues (e.g., base rates, opponents' defense abilities) for allocating the ball so as to win games.

The cold hand

The hot hand belief is generally based on the notion that success motivates people, through raising their self-confidence, to keep doing well or sometimes to even do better. Whether investigating the hot hand, clutch hitting,⁹ choking,¹⁰ or the cold-foot phenomenon, sports research finds the psychological effects noticeably important. Being close to the hot hand derivative, we find the cold hand/foot deserves appropriate attention as well.

As mentioned earlier in this review, Tversky and Gilovich (1989b) found that a time delay between shots had no effect on the probability of success for basketball players, and hence, cannot be blamed for masking the hot hand. Later, Berry and Wood (2004) examined the effect of a time-out interval on the probability of success for field goal kickers on a "pressure" kick (i.e., a kick considered to be critical to the outcome of the game), and provided a somewhat different conclusion. It was assumed that when allowing the kicker enough time (an extra 2 min in this case) to think about the importance of his upcoming kick, his probability of success decreases (i.e., icing the kicker). Using a multi-variable model accounting for different kickers, the distance of the kick, the turf type, indoor/outdoor games, and weather conditions, allowed for better isolation of the possible effects of pressure and icing. Analyzing all pressure kicks during the 2002 and 2003 National Football League (NFL) seasons, Berry and Wood found that icing the kicker had a quite strong negative effect depending upon the distance of the kick, and thus is indeed a successful strategy to be used in games. The effect of other factors examined, including the second psychological variable (pressure), was relatively minor. However, one should consider the significance of the results obtained in the study in light of the small sample size (38) of icing attempts.

Evaluation procedure

Finally, since the outcomes of hot hand studies vary from seemingly support to seemingly negation of the hot hand phenomenon, we find that evaluation of individual studies is essential and valuable for future research. This is in comparison with considering an "overall picture" of the results obtained (i.e., the combined research results). For example, no hot hands could be detected in field goal data for nine major players of the Philadelphia 76ers during the 1980–1981 season (Gilovich et al., 1985, Study 2), while field goal data of 123 NBA players during the

⁹Clutch hitting refers to substantial elevated performance under pressure circumstances.

¹⁰Choking is defined as performance decrements under pressure circumstances (Baumeister, 1984).

1989–1990 season indicated that 17 were streak shooters (Forthofer, 1991). Such conflicting results obtained from the same sport studied (i.e., basketball) and apparently with the same task performed (i.e., field goal shooting) raises an essential question regarding the validity of hot hand definitions applied by the researchers. Combining the results of both studies so as to estimate the effect size for the hot hand would blur such observations, which are more important to discuss than the overall magnitude of the effect. Even if one considers employing a quantitative procedure that seems relevant to our discussion (i.e., estimating the effect size for the hot hand over a large number of observations), the figures obtained either in one direction or in the opposite, would hardly convince us about the existence or non-existence of the hot hand. Following Wardrop's (1998) suggestions, progress is required in a few important aspects of hot hand research (e.g., improving modeling processes), rather than focusing on what we label the results. In sum, we believe that at the present stage of hot hand research the traditional narrative approach (i.e., listing and describing conflicting research findings) is preferable. The controversy between numbers and intuition is yet to be solved, and thus it is suggested that the hot hand should still be regarded as an open question.

Concluding remarks

In this review we have presented the more important studies that investigated the hot hand in sports. Our survey included both the empirical research, based on real data, and statistical examinations of simulated data. Although the issue has been extensively discussed in the last two decades, the question of whether success breeds success and failure breeds failure remains unsolved. Apparently, most of the empirical research supports Gilovich et al.'s (1985) argument concerning the non-existence of a relationship between future success and past performance (the sequential dependence claim). This has been strongly evident in professional basketball and in a few other sports. However, simulation studies demonstrate that fluctuations in success rates are present (the non-stationarity claim), and that the conventional tests in use are often unable to detect them.

In light of the conflicting outcomes of the studies presented in this review, we think a step further needs to be taken. First, the debate should be shifted from the search for evidence for or against the existence of the hot hand to a profound discussion about the norms used by statisticians, psychologists, and sports people. Such an approach may promote a better understanding of the issue, especially if at first glance conclusions seem to be contradictory. Second, further theoretical progress around the structure of the environment in which a hot hand belief is likely to emerge or change is also needed, as has already been proposed by Burns (2004). An important step forward, then, would be to detect the situational factors that enable us to judge the value of the belief (a fallacy vs. an adaptive strategy) for decision-making. Finally, a research strategy that validates the scientific debate's importance to real life decisions in sports (such as betting, allocation decisions, etc.) is required. Such a strategy would allow us to become prescriptive in this research field for many specific situations, sports, or decision-making problems.

Koehler and Conley (2003) asserted that no single study could be the last word on this topic. It may well be that hot hands do exist, but their presence is affected by factors related to the nature

of the task performed, the level of expertise, or some psychological (or emotional) variable. If streak hitters or shooters do exist, future research should identify the conditions in which they may emerge. On the other hand, if athletic performance is unconditionally not elevated due to past success, obviously the mental techniques (recommended by sport psychologists) commonly used in both training and competitions should be reconsidered.

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